

Fig. 6.— ΔpK as a function of acid strength: \diamond , substituted anilines; \square , amines; \blacklozenge , ketones; \triangle , phenols and alcohols (data of D. C. Martin and J. A. V. Butler (*J. Chem. Soc.*, 1366 (1939), and P. Ballinger and F. A. Long, *THIS JOURNAL*, 81, 1050, 2347 (1959).); \circ , carboxylic acids; \bullet , $MO_x(OH)_y$.

H_2CO_3 is abnormally low. This is due to the fact that an appreciable contribution to the acidity of carbonic acid comes from dissolved CO_2 . Our point for *p*-nitrodiphenylamine appears to be somewhat low. The experimental uncertainty in ΔpK is large for this indicator and no conclusions can be drawn at present for ΔpK for amines with pK values less than zero.

In solutions concentrated in sulfuric acid, medium effects on ΔpK are to be expected. These arise in part from the correction necessary to equation 8 from the relative fugacities of H_2O and D_2O in H_2SO_4 and D_2SO_4 , respectively. Furthermore reactions of the type



become of importance. Even in the approximations used in equation 8 we would find

$$\Delta pK = \log f_{BD^+} + \log f_{D_2SO_4} - \log f_{D_2SO_4^+} \quad (17)$$

These effects may be responsible for the drop in ΔpK for the substituted anilines with negative pK values.

NOTE ADDED IN PROOF.—Bascombe and Bell (*J. Chem. Soc.*, 1096 (1959)) have recently reported measurements of pK (H_2O solutions) for some of the indicators studied by us. Their measurements include solutions of H_2SO_4 among a number of different acids. Wherever comparisons can be made, our values of pK and H_0 are in agreement with those of Bascombe and Bell. For the indicator *p*-nitrodiphenylamine they find a medium and wave length effect on pK and H_0 . From three different assumptions, pK and H_0 are calculated from measurements at 4100 Å. H_0 is less sensitive to the nature of the assumption than pK . Our values of pK , H_0 , and D_0 were obtained from measurements at 4100 Å. The medium effects observed by Bascombe and Bell for this indicator probably explain the fact that our value of ΔpK for this indicator is anomalously low.

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Ion Pairs. I. Isotope Effects Shown by Chloride Solutions in Glacial Acetic Acid¹

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Appreciable isotopic separation has been obtained in countercurrent columns using the distribution of chlorine between HCl gas and solutions of inorganic chlorides in glacial acetic acid. The isotope effects³ vs. Cl atoms, calculated from the observed enrichments for various species present in the solutions are: HCl (dissolved), 1.0050 ± 0.0002 ; $HgCl_2$, 1.0061 ± 0.0009 ; $HCl \cdot H_2O$, 1.0039 ± 0.0003 ; $SrCl_2$, 1.0042 ± 0.0003 ; $LiCl$, 1.0040 ± 0.0003 . These results are consistent with a picture involving strong $Hg-Cl$ bonds, but much "looser" interaction between the metal and chlorine atoms in the ion pairs from $LiCl$ and $SrCl_2$.

Introduction

This is the first in a series of papers describing experiments designed to provide a more detailed understanding of the nature of ion pairs in solvents

(1) This work was supported by the William F. Milton Fund of Harvard University. It was presented at the September 1958 American Chemical Society meeting in Chicago.

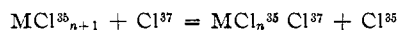
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(3) The isotope effect for a given species is the equilibrium constant, corrected for symmetry, for the isotopic exchange reaction with free atoms. It is numerically equal to the Cl^{37}/Cl^{36} ratio which would be present in the species in equilibrium with equal concentrations of free gaseous Cl^{37} and Cl^{36} atoms.

of low dielectric constant. Most previous investigations have been concerned primarily with the dissociation constants of ion pairs. Data on at least three other general aspects of ion pairs should also be available to complete the picture: 1, average vibration frequencies and the stiffness of the bonding present, 2, the lability of various ion pairs as measured by rates of isotopic exchange, and 3, the effects of other salts on the activity coefficients of ion pairs. Such information should prove useful in interpreting kinetic data for organic reactions which apparently involve intermediates with con-

siderable charge separation such as carbonium ions. This paper presents some data bearing on points 1 and 2 above for various inorganic chlorides in glacial acetic acid obtained by the use of countercurrent columns adapted to the separation of chlorine isotopes. Such countercurrent columns provide a means of measuring the small isotope effects shown by chlorine, which are in turn related to the average stiffness of the vibrations in which the chlorine atoms are involved. In addition such columns, which provide efficient contact between liquid and gas phases together with continuous separation, can yield fairly large lower limits for the rates of the rapid isotopic exchange reactions of ion pairs.

The shifts of vibration frequencies upon isotopic substitution have been widely studied both experimentally and theoretically,⁴ principally to aid in the interpretation of complex spectra. Both exact expressions^{5,6} and convenient approximate relations⁶ are available for the resulting changes in partition functions. The isotope effect for a given species is by convention the equilibrium constant, corrected for symmetry, for an isotopic exchange reaction with free atoms such as



which is given by the appropriate ratio of partition functions. Such corrected equilibrium constants are unity in the classical limit, so that it is only the deviations from classical behavior, and principally only the stiffest vibrations involving the isotopic atom, which contribute to the observed isotope effects. Isotope effects often are calculated from vibration frequencies observed spectroscopically, but where spectroscopic data are lacking, the reverse calculation can give some sort of average of the highest vibration frequencies involved. Direct spectroscopic observation of the vibration frequencies of ion pairs in solution will be very difficult and possibly impossible due to a combination of absorption by the solvent and broadening of the lines due to strong interactions with the solvent.

Experimental

The principal part of the apparatus used was a 135 cm. column, 1 cm. in diameter, packed with $1/16$ inch glass helices. A stream of HCl gas was passed in at the bottom of this column while the chloride solution flowed down the column. At the top of this column was a device for sampling the gas phase, and above this a shorter column in which reflux was obtained by reaction of the HCl with an appropriate solution flowing in at the top of the column, usually a solution of an acetate in acetic acid.

This essentially simple apparatus was complicated by a number of less important but necessary additional features. A cartesian manostat was used to maintain a constant low pressure (usually about 210 mm.) thus reducing the solubility of HCl in the solutions. An indicator such as *p*-naphtholbenzein or cupric ion was added to the solutions so that the point of reflux could be observed and regulated (within a 25 cm. range near the bottom of the upper column). A slow adjustable leak out at the top of the column was necessary to compensate for air carried into the column with the solution and any other leaks at joints or stopcocks. A flowmeter and needle valve (glass and Teflon) were used to regulate the flow of solution (within $\pm 10\%$). At the bottom of the column excess HCl bubbled out through a

portion of the solution so that the HCl supply did not require precise regulation. The bottom of the column was also designed so that a measured portion of the solution could be isolated and removed for titration of the dissolved HCl with a solution of lithium acetate in glacial acetic acid.

Two HCl samples were taken from most runs, at least one of them long before the column had reached equilibrium so that the number of theoretical plates present could be calculated from the observed rate of approach to equilibrium. The samples were treated with dimethyl sulfate.⁷ The methyl chloride produced was separated from unreacted HCl and analyzed in an isotope ratio mass spectrometer (Consolidated-Nier, model 21-201). A standard sample of methyl chloride was run along with each of the samples. The instrument gave directly the ratio of the mass 52 peak to the sum of peaks 53, 51, 50, 49, 48 and part of 47, from which, using the ratio given by the standard methyl chloride, the percentage decrease in the $\text{Cl}^{37}/\text{Cl}^{35}$ ratio was calculated. Thus a positive enrichment corresponds to a favoring of the heavy isotope in the solution compared to HCl gas.

The equations describing the approach of a countercurrent column to equilibrium have been derived by Cohen.⁸ His equations need only slight modification to adapt them to the case of chlorine in which both isotopes are present in appreciable quantity. After the enrichment has reached about $1/3$ of the equilibrium value only one term of the Fourier expansion used in the solution is important, giving the simple solution

$$X_t = X_\infty(1 - Ae^{Bt})$$

where X_t is the per cent. enrichment at time t , " A " depends only on the amount of holdup in the column above the point of sampling, and " B " is inversely proportional to the number of theoretical plates present. From the two values of X for each run it was possible to calculate both X_∞ and " B " by successive approximations using Newton's method or from a table constructed for the case where one time was a factor of 3 longer than the other. Since the point of reflux varied during each run, the value of A is somewhat uncertain, and calculations were made for both 10 and 20% of the chlorine present above the point of sampling, giving values for " A " of 0.89 and 0.96, respectively. The results of the calculations are tabulated in terms of the H.E.T.P. (height equivalent theoretical plate, or column length per theoretical plate), and ϵ , the deviation of the single stage fractionation factor from unity.

Results

The type of data obtainable is shown in Fig. 1 which shows the results of a series of blank runs with no solutes other than HCl and H_2O present. The observed enrichments are plotted against the square root of a normalized time, the normalization factor, θ , being the holdup of the column divided by the flow rate. It is clear that water has a marked effect on the observed enrichments, even to changing the sign at concentrations above 1.5 M , at which point the solubility of HCl has increased to about twice its value in dry acetic acid. If all the increase in solubility is formally ascribed to the species H_3OCl , an essentially linear relation is obtained between the observed values of ϵ and the fraction of the dissolved HCl present as either HCl or H_3OCl as shown in Fig. 2. The effect of small quantities of water, under 0.1 M , should be negligible, and since excess acetic anhydride used as a drying agent had a larger effect, most runs were made with small amounts of water present.

The results of calculations for the five blank runs with almost dry acetic acid are listed in part A of

(7) This is an adaptation of the procedure given by H. R. Owen and O. A. Schaeffer, *THIS JOURNAL*, **77**, 898 (1955). The conversion to methyl chloride was not quantitative, however, in agreement with the results of Owen and Schaeffer, any isotopic fractionation in the conversion was less than the limits of experimental error in the mass spectrometric determination, about $\pm 0.2\%$.

(8) K. Cohen, "The Theory of Isotope Separation," National Nuclear Energy Series III-1B.

(4) E. B. Wilson, Jr., J. C. Decius and P. C. Cross, "Molecular Vibrations," McGraw-Hill Book Co., New York, N. Y., 1955.

(5) H. C. Urey, *J. Chem. Soc.*, 562 (1947).

(6) J. Bigeleisen and M. G. Mayer, *J. Chem. Phys.*, **15**, 261 (1947).

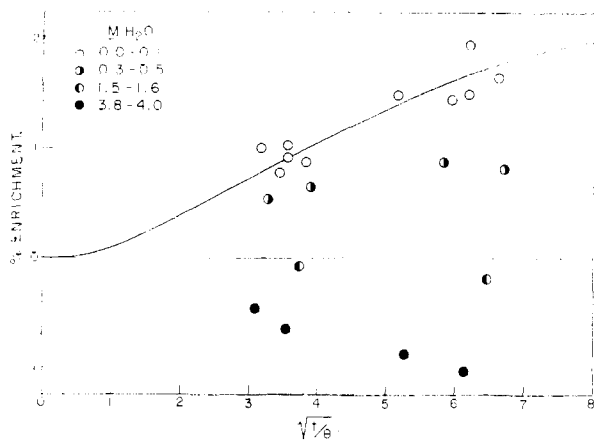


Fig. 1.—Observed isotopic enrichments in runs with HCl alone and with HCl·H₂O present vs. $\sqrt{t/\theta}$, where t/θ is a normalized time of operation of the column.

Table I. The average of the values for the isotope effect (dissolved HCl vs. HCl gas) is 1.00044, and a range of ± 0.00016 includes the results of almost all the individual calculations. The solid curve in Fig. 1 calculated for $\epsilon = 0.00044$ and a value of 50 theoretical plates fits the experimental points quite well.

The runs with mercuric chloride present at a concentration of about 0.15 *M* listed in part C of Table I show ultimate enrichments comparable to the blank runs, but a somewhat faster approach to equilibrium. This indication of a larger isotope effect balanced by a decrease in the number of theoretical plates is borne out by the calculations which yield a value for ϵ of 0.00079 ± 0.00025 . Dissolved HCl is still the principal species in these solutions, and a long extrapolation is necessary to obtain the value of 1.0015 ± 0.0009 for the isotope effect for HgCl₂. Converting to the usual standard of chlorine atoms instead of HCl gas gives the value of 1.0061 ± 0.0009 . (The value of 1.0046 for the isotope effect of HCl gas calculated by Urey⁵ was used for this conversion.) This is in satisfactory agreement with the value of 1.007 calculated for HgCl₂ gas from its known vibration frequencies.⁹

Both LiCl and SrCl₂ which are more soluble than HgCl₂ were studied over a wider range of concentration with the results listed in parts D and E of Table I. With both of these species, as with H₃OCl, the isotope effect is in the opposite direction from dissolved HCl, giving large cancellations and only small observed enrichments. The experimental error is too large a fraction of the observed enrichments to permit meaningful calculations of both the isotope effect and the number of theoretical plates from each single run as was done with the HgCl₂ data. Assuming a value of 25 theoretical plates leads to the values for ϵ shown in Fig. 2 which extrapolate to give isotope effects vs. chlorine atoms of 1.0040, 1.0042 and 1.0039 for LiCl, SrCl₂ and H₃OCl, respectively, with an uncertainty of ± 0.0003 in each case. These extrapolated values are not very sensitive to the value used for the number of theoretical plates. The presence of a change in sign of the observed enrichments at

(9) W. Klemperer and L. Lindeman, *J. Chem. Phys.*, **25**, 397 (1956).

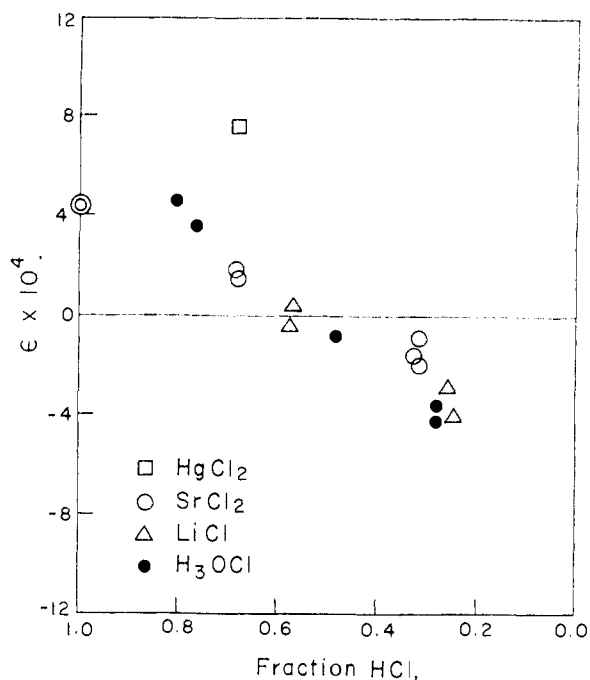


Fig. 2.—Plot of ϵ vs. the composition of the liquid phase. The observed single stage enrichment factors are equal to $1 + \epsilon$.

concentrations corresponding to a fraction of HCl of about 0.5 to 0.6, which is clearly evident in all three cases, is sufficient to fix the intercept within the range of -0.0003 to -0.0010 for ϵ or 1.0043 to 1.0036 for the isotope effect vs. chlorine atoms. The smallest value for the number of theoretical plates which would still give a roughly linear dependence of ϵ on the fraction of the chlorine present as HCl is about 8. A value of less than 8 would lead to over 99% of the equilibrium enrichment in 60 minutes and so is also inconsistent with the observed further enrichments at longer times.

Discussion

The Cl³⁷/Cl³⁵ isotope effect for the LiCl gaseous molecule can be calculated from the LiCl³⁵ vibration frequency,¹⁰ giving the value 1.0035. The contribution of the LiCl bond to the isotope effect should be considerably decreased in a dielectric, and thus most of the observed value of 1.0040 for LiCl dissolved in glacial acetic acid must be ascribed to the vibrations involved in the solvation of the chloride ion. The increase in the isotope effect in going from HCl gas to dissolved HCl must also be due to solvation, and the isotope effect observed for H₃OCl further demonstrates that O—H—Cl hydrogen bonds may make a sizable contribution. The numerical agreement of the values for LiCl, SrCl₂ and H₃OCl may be coincidental, or it may be a valid indication that these species exist in glacial acetic acid solutions in a "solvent separated" form with the cation sufficiently distant that it is not importantly involved in the vibrations of the chloride ion. The presence of strong Hg—Cl bonds in acetic acid solutions of

(10) W. Klemperer and S. A. Rice, *J. Chem. Phys.*, **26**, 618 (1957).

TABLE I

	HCl, <i>M</i>	H ₂ O, <i>M</i>	Flow ^a rate	Time, min.	% enrich.	H.E.T.P., ^c		$\epsilon \times 10^4$ ^c		
						<i>b</i>	<i>c</i>	<i>b</i>	<i>c</i>	
(A)	0.64	0.08	3	60	0.78	2.0	3.8	3.1	5.1	
				180	1.45					
	.33 ^d	.1 ^e	4	60	0.92	3.6	5.2	4.1	6.3	
				180	1.49					
	.65	.08	4	60	1.03	1.5	3.2	3.5	6.0	
				180	1.95					
	.56	.09	4.5	60	0.88	1.5	3.0	2.7	4.6	
				180	1.65					
	.50	.09	6	40	1.00	5.6	7.8	(6.7)	(9.0)	
				107	1.49					
								Av.	4.4 ± 1.6	
(B)	H ₃ OCl, <i>M</i>									
	0.13	0.5 ^e	6	60	0.65	6.6	8.7	4.0	5.2	
				180	.81					
	.19	.6 ^e	4	60	.54	4.4	6.4	3.2	4.5	
				190	.88					
	.62	.6 ^e	5.5	60	-.08	5.4 ^e		-0.8		
				180	-.19					
	1.5	.6 ^e	3	60	-.46	5.4 ^e	4.3	-3.9	-3.7	
				180	-.88					
	1.6	.6 ^e	3.9	4.5	60	-.65	4.0	5.8	-3.4	-4.8
180				-1.03						
								Av.	7.9 ± 2.5	
(C)	HgCl ₂ , <i>N</i>									
	0.32	0.67	0.08	3	60	0.88	4.4	6.6	5.7	8.3
				180	1.49					
	.32	.40 ^d	.11	3	60	1.03	3.9	6.0	6.1	9.0
					180	1.76				
	.30	.69	.14	3.5	60	1.11	4.8	6.9	6.9	9.8
					180	1.76				
	.31	.55	.14	4	60	1.23	4.9	6.9	7.6	10.6
					180	1.91				
	.35	.6 ^e	.1 ^e	5.5	75	1.57	4.6	6.5	8.0	11.2
					195	2.18				
	.31	.63	.14	4	60	1.19	4.5	6.3	6.7	9.3
					180	1.84				
	.23	.49	.1 ^e	5.5	60	0.96	7.1	9.6	6.3	8.5
					120	1.15				
	.32	.72	.11	5.5	65	1.03	3.2	4.7	4.3	6.2
155					1.53					
.23	.64	.1 ^e	5.5	50	0.84	11.1	14.6	7.9	10.4	
				150	0.96					
								Av.	7.9 ± 2.5	
(D)	LiCl, <i>M</i>									
	0.53	0.70	0.04	3	180	0.08	5.4 ^e		0.4	
				60	.00					
	0.53	.72	.04	4	144	-.08	5.4 ^e		-0.4	
					60	-.23				
	2.0	.66	.07	2	60	-.77	5.4 ^e		-4.0	
180					-.27					
2.0	.70	.07	2	60	-.50	4.0	7.5	-2.2	-3.5	
				180	-.50					
								Av.	7.9 ± 2.5	
(E)	SrCl ₂ , <i>N</i>									
	0.30	0.64	0.09	2	60	0.23	5.4 ^e		1.5	
				180	.31					
	0.30	.65	.09	4	60	.38	5.4 ^e		1.8	
					180	.42				
	1.6	.74	.0 ^e	1	240	-.31	5.4 ^e		-1.6	
					60	-.11				
	1.6	.77	.0 ^e	2	180	-.19	5.4 ^e		-0.9	
60					-.27					
1.6	.74	.0 ^e	2	60	-.46	4.0	6.0	-1.6	-2.3	
				180	-.46					

^a Flow rate in ml. min.⁻¹ cm.⁻². ^b Values in this column were calculated on the basis of 10% of the total holdup present above the point of sampling, *i.e.*, $A = 0.89$. ^c Values in this column were calculated assuming that the amount of holdup above the point of sampling is 20% of the total holdup, *i.e.*, $A = 0.96$. ^d These two runs were made at a pressure of about 130 mm. instead of approximately 210 mm. as used for the other runs. ^e These values were not directly measured or calculated but are estimated from corresponding figures in other runs. ^f This run was made in a column packed with Podbelniak Heli-Pak 3014 instead of Pyrex helices.

HgCl₂ is to be expected since HgCl₂ is largely un-ionized even in water solutions.

An isotope effect of about 1.0040 for a solvated chloride ion is not inconsistent with the limited data available on the vibration frequencies of O-H-Cl hydrogen bonds¹¹ as is shown by the approximate calculation to be given. The relations between the frequencies of stretching vibrations and the masses and force constants involved for a linear triatomic system are given by Herzberg¹² as $4\pi^2(\nu_1^2 + \nu_3^2) = k_1(1/m_x + 1/m_y) + k_2(1/m_y + 1/m_z)$ and $16\pi^4\nu_1^2\nu_3^2 = k_1k_2(m_x + m_y + m_z)/m_x \cdot m_y m_z$. For hydrogen bonds in which the mass of the central atom, m_y , is considerably smaller than the other two, one of the frequencies, ν_3 , hereinafter called the hydrogen stretching frequency, will be considerably higher than the other, and a sufficiently accurate solution is $4\pi^2\nu_3^2 = (k_1 + k_2)/m_y + (1/m_x)(k_1^2/(k_1 + k_2)) + (1/m_z)(k_2^2/(k_1 + k_2))$ and $4\pi^2\nu_1^2 = ((m_x + m_y + m_z)/m_x m_z)(k_1 k_2/(k_1 + k_2))$. k_1 is the force constant for stretching the x-y bond and k_2 refers to the y-z bond. These expressions are readily differentiated with respect to m_z , and then multiplying by $\Delta m_z = 2$ awu, one obtains the changes in frequency on changing from Cl³⁵ to Cl³⁷. Substituting directly into Bigeleisen's equations⁶ one obtains

$$\epsilon = \sum_i G(u_i) \Delta u_i = n \left(\frac{1}{8\pi^2} \right) \left(\frac{h}{kT} \right)^2 \left(\frac{k_2 \Delta m_z}{m_z^2} \right) \left(\frac{k_1 G(u_1)}{(k_1 + k_2) u_1} + \frac{k_2 G(u_3)}{(k_1 + k_2) u_3} \right)$$

for the isotope effect due to n hydrogen bonds to the Cl⁻ ion. $u_i = h\nu_i/kT$ and $G(u)$ is a function tabulated by Bigeleisen.⁶ u_1 lies in the range for which $G(u)/u = 1/12$ is a valid approximation; however $G(u_3)/u_3$ must be obtained by successive approximations, or the value of 0.041 calculated from the hydrogen stretching frequency in the HCl-methyl ether complex,¹¹ may be used. k_2 is probably considerably smaller than k_1 due to the lower charge density on a chlorine atom as compared to an oxygen atom. Assuming that $k_1 = 1.5k_2$ ¹³ and putting in the experimentally determined isotope effect, one obtains: $\epsilon = 0.0040 = nk_2(3.19 \times 10^{-7})[(3/5) 0.083 + (2/5) 0.041]$ and $nk_2 = 1.9 \times 10^5$ dynes cm.⁻¹¹⁴ The hydrogen

(11) G. L. Vidale and R. C. Taylor, *THIS JOURNAL*, **78**, 294 (1956).

(12) G. Herzberg, "Infrared and Raman Spectra of Polyatomic Molecules," D. Van Nostrand Co. Inc., New York, N. Y., 1945.

(13) The assumption that $k_1 = k_2$ gives $nk_2 = 2.0_8 \times 10^5$ and an estimate of 1.4 for n .

(14) The approximations used in the above calculations are similar to those used by Bigeleisen and Mayer⁶ for SnCl₄, etc. Unfortunately their equations cannot be used directly in the present case because of the high frequency of the hydrogen stretching vibrations.

stretching vibrations of O-H-Cl hydrogen bonds have been observed in HCl-methyl ether complexes¹¹ at about 2250 cm.⁻¹, corresponding to $k_1 + k_2 = 3 \times 10^5$, which in turn gives an estimate of 1.6 for n , the number of hydrogen bonds per Cl atom. A similar estimate can be made for the aqueous chloride ion, based on the isotopic enrichment data of Urey, *et al.*¹⁵ Assuming that their column gave a H.E.T.P. between 0 and 15 cm., the isotope effect for aqueous chloride ion is in the range of 1.0043 ± 0.0003 , which gives $nk_2 = 2.0_3 \times 10^5$ and an estimate of 1.7 for n .

TABLE II

	H.E.T.P.	$\tau,^b$ sec.	$k_2,^c$ l. mole ⁻¹ sec. ⁻¹
HgCl ₂	0.3 N	6	0.079
LiCl	2.0 M	17 ^a	.014
SrCl ₂	1.6 N	17 ^a	.036

^a Maximum value for the H.E.T.P. consistent with the data. ^b Maximum value for the half time for isotopic exchange with HCl present at 0.6 to 0.7 M. ^c Minimum value for the rate constant for exchange assuming second-order kinetics.

The rate of isotopic exchange reactions within the liquid phase is only one of a number of factors determining the H.E.T.P. Some of these contributions are additive, but there is a complicated interaction between the exchange reactions and mixing and diffusion processes in the liquid phase. Not enough is known about the flow in packed columns to calculate the effect of this interaction; however a lower limit for the rate of isotopic exchange can be calculated by neglecting all contributions to the H.E.T.P. other than that of the exchange reaction. The results of this calculation are summarized in Table II. There is an additional uncertainty in the LiCl and SrCl₂ results due to the smallness of the observed enrichments, and the maximum value for the H.E.T.P. consistent with the data, 17 cm., has been used to get an absolute minimum for the exchange rates. The H.E.T.P.'s for the HgCl₂ runs are only slightly larger than those of the blank, HCl only, runs, so the exchange rate is probably much faster than the calculated minimum. A study of the HCl-acetyl chloride exchange in the same columns at various concentrations of ZnCl₂ catalyst is under way in this Laboratory and eventually should permit the setting of higher minimum values for the exchange reactions reported here.

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(15) H. D. Urey, A. Mills, I. Roberts, H. G. Thode and J. R. Huffman, *J. Chem. Phys.*, **7**, 138 (1939).